

Leave
blank

1. Simplify

(a) $(3\sqrt{7})^2$ **(1)**

(b) $(8+\sqrt{5})(2-\sqrt{5})$ **(3)**

(Total 4 marks)

Q1



2. Given that $32\sqrt{2} = 2^a$, find the value of a .

(3)

Leave
blank

Q2

(Total 3 marks)

3

Turn over



H 3 4 2 6 2 A 0 3 2 8

3. Given that $y = 2x^3 + \frac{3}{x^2}$, $x \neq 0$, find

(a) $\frac{dy}{dx}$ **(3)**

(b) $\int y \, dx$, simplifying each term. **(3)**



8.

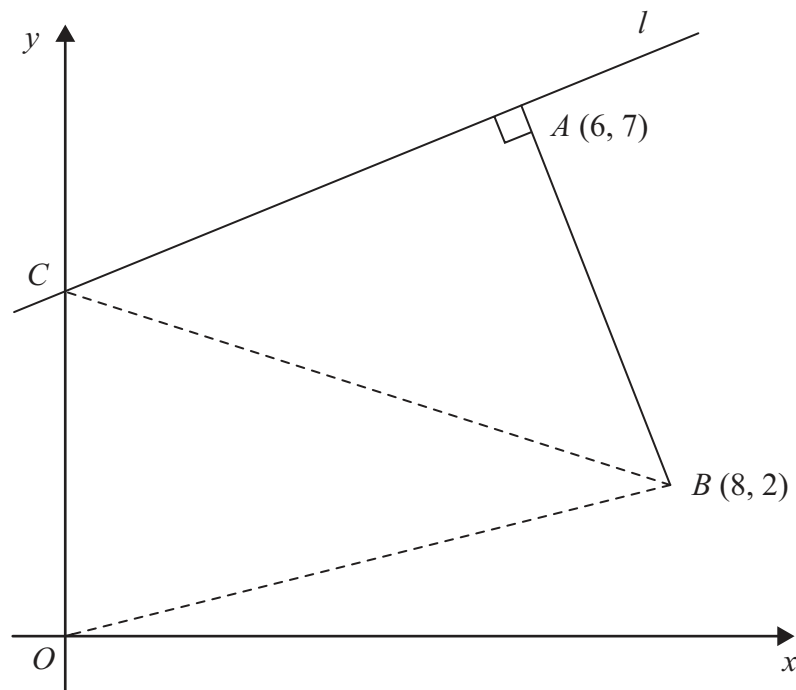


Figure 1

The points A and B have coordinates $(6, 7)$ and $(8, 2)$ respectively.

The line l passes through the point A and is perpendicular to the line AB , as shown in Figure 1.

(a) Find an equation for l in the form $ax + by + c = 0$, where a , b and c are integers. (4)

Given that l intersects the y -axis at the point C , find

(b) the coordinates of C , (2)

(c) the area of $\triangle OCB$, where O is the origin. (2)





Question 9 continued

Leave
blank

Lined area for writing the answer to Question 9.



H 3 4 2 6 2 A 0 2 0 2 8

Leave blank

10. (a) Factorise completely $x^3 - 6x^2 + 9x$ **(3)**

(b) Sketch the curve with equation

$$y = x^3 - 6x^2 + 9x$$

showing the coordinates of the points at which the curve meets the x -axis.

(4)

Using your answer to part (b), or otherwise,

(c) sketch, on a separate diagram, the curve with equation

$$y = (x - 2)^3 - 6(x - 2)^2 + 9(x - 2)$$

showing the coordinates of the points at which the curve meets the x -axis.

(2)



Question 10 continued

Leave
blank



23

Turn over

Question 10 continued

Leave
blank



Question 10 continued

Leave
blank

(Total 9 marks)

Q10

25

Turn over



11. The curve C has equation

$$y = x^3 - 2x^2 - x + 9, \quad x > 0$$

The point P has coordinates $(2, 7)$.

- (a) Show that P lies on C . (1)

- (b) Find the equation of the tangent to C at P , giving your answer in the form $y = mx + c$, where m and c are constants. (5)

The point Q also lies on C .

Given that the tangent to C at Q is perpendicular to the tangent to C at P ,

- (c) show that the x -coordinate of Q is $\frac{1}{3}(2 + \sqrt{6})$. (5)



